# Key Agreement Scheme Based on Smart Cards 

Graygorry Brayone Ekal ${ }^{\text {a,1,** }}$, Eddie Shahril Ismail ${ }^{\text {a,2 }}$, Abdul Rahman Farhan bin Sabdin ${ }^{\text {a,3 }}$<br>${ }^{\text {a }}$ Department of Mathematical Sciences, Universiti Kebangsaan Malaysia, 43600 UKM Bangi, Selangor, Malaysia<br>${ }^{1}$ graygorrybrayone@gmail.com*; ${ }^{2}$ esbi@ukm.edu.my; ${ }^{3}$ a168637@siswa.ukm.edu.my<br>* Corresponding author

## ARTICLE INFO

## Keywords

Cryptography
Key agreement
Smart card
Global mobility network
Roaming


#### Abstract

An efficient roaming service over wireless networks is essential for mobile users. It allows mobile users to seamlessly access the services provided by the home agent without losing connectivity when they visit a foreign network. This handover communication happens with the help of a foreign agent. In most cases, the communication between the mobile user and the foreign agent occurs over an unsecured channel. Therefore, researchers have proposed various authentication schemes to protect data transmitted over this unsecured channel. Most of the proposed schemes are focused on key agreement schemes. However, the key agreement schemes researchers have submitted are primarily high in computational and communication costs. Therefore, this research proposed an authenticated key agreement scheme based on passwords and smart cards with lower computational and communication costs without compromising the scheme's security. This criterion was achieved due to using lower-cost operations and functions in the scheme. Moreover, the scheme's development is based on the result of analyzing and improving other schemes proposed by other researchers.


## 1. Introduction

Nowadays, wireless communication has become essential in various aspects of our life. For instance, transferring money from one person to another can be done anywhere through online banking without going to the bank. Furthermore, users can enjoy online shopping and communicate with each other wherever they are around the world, anytime they want. The ability of users to present at any place and still can access these services is facilitated by the global mobility network through roaming service [1]. In the global mobility network, there are three entities involved, namely "mobile user", "home agent", and "foreign agent" [2].

Moreover, the terms home network and foreign network are used throughout this paper. A home network is a network that is the permanent home of the mobile user. Meanwhile, a foreign network is a network to which the mobile user moves outside their home network coverage area. Next, a mobile user is a person from a home network who uses devices such as a mobile phone, laptop, or tablet. Next, home and foreign agents are routers at home and foreign networks, respectively [3]. The mobile user needs to register themselves at the home agent via a secured channel before they get
their desired services. However, when the mobile user visits a foreign network, they must send a request to the foreign agent to use the services provided by the home agent.

Wireless signals are open and public; thus, the data transmission between the mobile user, the home agent, and the foreign agent is vulnerable to attacks from unauthorized parties. Hence, it is crucial to employ proper security protocols, which as roaming authentication, to resist attacks or overcome other protocol weaknesses [1]. If the mobile user is in their registered network, the home agent can verify the mobile user's authenticity. On the other hand, if the mobile user is in a foreign network, the foreign agent cannot directly authenticate the mobile user because it does not have the credentials of the mobile user. Therefore, through roaming authentication, the foreign agent is able to confirm the legitimacy of the mobile user with help from the home agent. A session key will be agreed upon between the foreign agent and the mobile user and will be used to secure the communication channel.

Apart from that, mobile devices are typically constrained in terms of computational power, battery lifetime, and communications (i.e., network bandwidth and mobility) [4], [5]. These weaknesses will affect the efficiency and effectiveness of the authentication prosses between the home agent, foreign agent, and mobile user. A secure and efficient key agreement scheme based on a smart card between the mobile user and a foreign agent was proposed to overcome the mobile device's limitations and security issues during roaming. The smart card is a subscriber identity module (SIM) that is directly integrated into the mobile device [6]; hence only the mobile user who possesses the smart card can pass the verification from the foreign agent and home agent. Smart cardbased authentication is used because of its simplicity, portability, and cryptographic capabilities [2], [7].

The remainder of the paper is organized as follows. In Section 2, other researchers' works are first observed and analyzed before relating the findings to this research's scheme. Then, in Section 3 , an overview of the mathematical concepts that are used to develop the key agreement scheme is explained. Section 4 presents the proposed scheme in detail. Next, Section 5 discusses the safety of the scheme. In addition, Section 6 shows the proposed scheme's performance and efficiency. Finally, conclusions regarding the findings are presented in Section 7.

## 2. Related Works

Over the past years, various researchers have proposed many smart card-based key agreement schemes for roaming services. Lamport [8] developed the first password authentication technique in 1981, which employed a safe hash function to generate one-time passwords for validating user identification. Furthermore, Aziz and Diffie [9] established a security-protecting authentication system for wireless networks using a random nonce and a user's certificate in 1994. Moreover, Park [10] introduced a certificate-based session key exchange mechanism for wireless mobile systems in 1997. Several years later, Zhu and Ma [11] introduced a novel authentication mechanism for wireless networks utilizing a smart card to improve security protocol. In their proposed scheme, mobile users are only required to conduct symmetric encryptions and decryptions, reducing the computational burden. However, it was pointed out by Lee et al. [12] that Zhu and Ma's scheme cannot accomplish full backward secrecy and mutual authentication, so they offered an upgrade to address the shortcomings of the scheme. Unfortunately, Lee et al.'s proposed authentication scheme was found by Xu et al. [13] to have several security flaws, namely non-anonymity, unequal key agreement, and the inapplicable security design. Therefore, a new authentication scheme for wireless networks that included anonymity was developed by Xu et al.

On the other hand, Karuppiah and Saravanan [14] devised an improved authentication scheme for roaming services by utilizing the one-way hash function, Diffie-Hellman problem, and discrete logarithm problem. This improved authentication scheme was developed in order to remedy the weaknesses the Rhee et al.'s scheme [15]. In 2017, Guo and Sun [16] developed a novel password-
based authentication scheme with a smart card. Their scheme only uses a hash function and exclusive-OR operations to encrypt and decrypt data exchanged between the mobile user, foreign agent, and home agent. Hence, they claim that their scheme is more efficient because of the absence of asymmetric and symmetric encryption/decryption while maintaining the scheme's security. Moreover, in 2018, Xu et al. [17] proposed a new efficient mutual authentication and key agreement scheme with smart card-based by implementing a low-cost cryptographic primitive, the ExclusiveOR operation. Furthermore, Pan et al. [18] proposed an enhanced secure smart card-based Password Authentication Scheme by implementing a biometric-based password authentication.

The authentication scheme in this paper is inspired by the authentication scheme developed by Guo and Sun [16]. Similar to the approaches by Guo and Sun, a low-cost cryptographic primitive, the exclusive-OR operation, and a one-way hash function was used to maintain the scheme's security. Moreover, the efficiency of Guo and Sun's scheme would be improved by reducing the number of operations and calculations involved without compromising the scheme's security.

## 3. The Proposed Method

This section will briefly introduce the cryptographic primitives (Exclusive-OR), and a function (hash function) used to develop the key agreement scheme. The Exclusive-OR operation is a tool to encrypt and decrypt every message transmitted between the mobile user, home agent, and foreign agent. Meanwhile, the one-way hash function is used for data integrity to ensure whether the message received is valid [19].

### 3.1.Exclusive-OR

Exclusive-OR (XOR) is a simple bitwise operation, denoted as $\oplus$ and operates on binary data. The idea behind this operator is that if two input bits are the same and XOR'ed, the output bit will be " 0 ". However, if two input bits differ, the output bit will be " 1 ". Furthermore, in cryptography, XOR operates on binary data such as one message bit and one key stream bit to generate one ciphertext bit [20]. Four important properties of the XOR operator are useful in cryptography. Given three inputs (in binary form), say $A, B$, and $C$. Then these following statements are true.

1) XOR operation is commutative;
$A \oplus B=B \oplus A$
2) XOR operation is associative;
$A \oplus(B \oplus C)=(A \oplus B) \oplus C$
3) There exists an identity element in XOR'ing which is " 0 ".
$A \oplus 0=A$
4) There exists an inverse for an element that is itself.
$A \oplus A=0$
The XOR encryption and decryption processes are given as follows [17]:

- Encryption process: plaintext $\oplus$ key $=$ ciphertext
- Decryption process: ciphertext $\oplus$ key = plaintext


### 3.2. Hash Function

Definition 1 (See [18]). A hash function is a function $h: x \rightarrow y$ that maps binary strings of arbitrary to binary strings of some fixed length, called hash-values. Note that $x$ is input in binary form, while $y$ is an output in binary form.

In order to be useful in cryptography, a hash function must be designed so that any two different inputs, say $x_{1}$ and $x_{2}$, cannot have the same hash value, say $h\left(x_{1}\right)=h\left(x_{2}\right)$. Furthermore, a hash function must be a one-way function meaning that it is easy to compute $h(x)=y$ for a given $x$, but difficult to compute $h^{-1}(y)=x$ for a given $y$ [14].

## 4. Proposed Scheme

This section presents the key agreement scheme for wireless roaming service based on smart cards. The proposed scheme will consist of three phases, namely the registration phase, login and authentication phase, and update password phase. The entities involved in this authentication process are mobile users, home agents, and foreign agents. Firstly, a mobile user who intends to roam to the foreign network must register with the home agent. A set of secret parameters saved on a smart card will be provided to the mobile user by the home agent. Then, the mobile user can use the smart card to $\log$ in to the home agent with the assistance of the foreign agent. After verifying that the mobile user is permitted, the home agent creates a session key between the mobile user and the foreign agent. In the update password phase, mobile use can change their password freely. The notations that are used throughout this section are listed in Table 1.

Table 1. Notations

| Notations | Descriptions |
| :--- | :--- |
| $A, B, C, D, E, F, G, H, I, J, K, L$ | Parameter |
| $A A$ | The home agent where the $P M$ registered |
| $A L$ | The foreign agent of a foreign network where the $P M$ visits |
| $I D_{A A}$ | The identity of the home agent |
| $I D_{A L}$ | The identity of the foreign agent |
| $I D_{P M}$ | The identity of the mobile user |
| $K P=[S, R, \ldots]$ | Smart card containing the parameter, say $S, R, \ldots$ |
| $N_{i}$ | The $i$-th nonce (a number that can only be used once $[21])$ |
| $P W_{P M}$ | A password of mobile user |
| $P M$ | A mobile user |
| $K S$ | Session key |
| $h(\cdot)$ | Hash function |
| $h_{k}(\cdot)$ | Keyed hash function |
| $\oplus$ | A XOR operation |
| $\\|$ | A concatenation operator |
| $\{\alpha, \beta, \ldots\}$ | A message that contains parameters say $\alpha, \beta, \ldots$ |

### 4.1.Registration Phase

Before a mobile user visits a foreign network, they must register with their home agents via a secure channel. In this phase, only two entities are involved: the mobile user and the home agent. The overview of the whole process of this phase is depicted in Table 2. The details are described as follows:

Step 1:PM $\rightarrow A A:\left\{I D_{P M}, A\right\}$

- $\quad P M$ will randomly pick a secrete number $b$
- Then he/she freely chooses his/her password $P W_{P M}$
- After that, $P M$ will compute a parameter $A$ such that $A=h\left(P W_{P M} \| b\right)$
- $\quad P M$ then sends $A$, and its $I D_{P M}$ to $A A$

Step 2:AA $\rightarrow P M: K P=[C, D, h(), x$.

- $A A$ received $A$ dan $I D_{P M}$ from $P M$.
- $\quad A A$ randomly generates a number $x$ and calculates the following parameters:
$B=h\left(I D_{A A} \| h_{k}(x)\right)$
$C=h\left(A \| I D_{P M}\right) \oplus B$
$D=h(B)$
- $A A$ the stores $C, D, h(),$.$x into the smart card, K P$, and send $K P$ to $P M$

Step $3: K P=[C, D, h(), x, b$.

- $\quad P M$ received $K P$ from $A A$
- $P M$ stores $b$ into $K P$

Table 2. Registration Phase


### 4.2. Login and Authentication Phase

When the mobile user visits a foreign network, they will undergo a login and authentication phase before they gain access to the services provided by their home network. In the login phase, $P M$ inserts their smart card, $K P$ into their mobile device. Then, $P M$ enters their password and identity, which is $P W_{P M}$ and $I D_{P M}$, respectively. To ensure the $P M$ is the owner of the $K P$, the $K P$ will perform an authentication procedure. If the $P M$ is the valid owner of that $K P$, then only the $A L$ can proceed to validate whether the $P M$ is the registered user of the $A A$ or not. In this phase, it is assumed that $A L$ and $A A$ already agreed with $h_{k}\left(I D_{A L} \| w\right)$ and $w$. Finally, if $P M$ is verified to be the registered user under the $A A$, then $A A$ will generate a session key, $K S$, to be used in the communication between $P M$ dan $A L$. The detailed process of the login and authentication phase will be depicted in Table 3 and explained as follows:

Step 1 : Verify the owner of the $K P$

- $\quad P M$ inserts their $I D_{P M}$ and $P W_{P M}$
- $K P$ then calculate the following parameters:

$$
\begin{aligned}
& A=h\left(P W_{P M} \| b\right) \\
& B=h\left(A \| I D_{P M}\right) \oplus C
\end{aligned}
$$

- $\quad K P$ checks $h(B) \stackrel{?}{=} D$
(If equal, then the $P M$ is the real owner of $K P$, and vice versa)

Step $2: P M \rightarrow A L:\{E, F, x\}$

- $P M$ generates a nonce, $N_{1}$.
- Then, $P M$ computes $E$ and $F$ using the calculated value $B$ as follows:

$$
\begin{aligned}
& E=N_{1} \oplus B \\
& F=h(E \| B)
\end{aligned}
$$

- $\quad P M$ sends $E, F, x$ to $A L$. The value $x$ is obtained from $K P$.

Step $3: A L \rightarrow A A:\{E, G, H, w, x\}$

- $A L$ receives $E, G, H, w, x$ from $P M$.
- $A L$ also generates a random nonce, $N_{2}$.
- $\quad A L$ then computes $G$ and $H$ as follows:

$$
\begin{aligned}
& G=N_{2} \oplus h_{k}\left(I D_{A L} \| w\right) \\
& H=F \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right)
\end{aligned}
$$

- After that, $A L$ sends $E, G, H, w, x$ to $A A$.

Step 4 : $A A$ checks the authenticity of the message $E, G$

- $A A$ receives $E, G, H, w, x$ from $A L$.
- $\quad A A$ uses the received $E, G, x, w$ to calculate:

$$
h\left(E \| h\left(I D_{A A} \| h_{k}(x)\right)\right) \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right)
$$

- $A A$ verifies whether $E, G$ are valid messages sent by $A L$ or not through the following comparison:

$$
h\left(E \| h\left(I D_{A A} \| h_{k}(x)\right)\right) \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right) \stackrel{?}{=} H
$$

Step 5 : The development of the session key, $K S$

- $A A$ uses the received $x, w, k$ to extract the nonces, $N_{1}$ and $N_{2}$ from $E$ and $G$, respectively, by performing the following calculation:

$$
\begin{aligned}
& N_{1}=E \oplus h\left(I D_{A A} \| h_{k}(x)\right) \\
& N_{2}=G \oplus h_{k}\left(I D_{A L} \| w\right)
\end{aligned}
$$

- The session key $K S$ is created by using the extracted nonces, $N_{1}$ and $N_{2}$ as follows:

$$
K S=h\left(N_{1} \oplus h_{k}(x) \| N_{2}\right)
$$

- This session key is stored inside the parameter $I$ :

$$
I=K S \oplus N_{2}
$$

Step $6: A A \rightarrow A L:\{I, J, K, L\}$

- $\quad A A$ also computes $J, K, L$ :

$$
\begin{aligned}
& J=h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right) \\
& K=N_{1} \oplus N_{2} \\
& L=h\left(K \| N_{2}\right)
\end{aligned}
$$

- $\quad I, J, K, L$ are then sent to $A L$.

Step 7 : $A L$ checks the validity of the parameters $I, K$, and derives the session key, $K S$, from $I$.

- $A L$ receives $I, J, K, L$ from $A A$.
- $A L$ calculate the following value by using $h_{k}\left(I D_{A L} \| w\right)$ :

$$
h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right)
$$

- Then, the validity of $I$ will be verified by calculating the following equation:

$$
h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right) \stackrel{?}{=} J
$$

- If $I$ is valid, then $A L$ can extract the session key, $K S$, from $I$ by using its $N_{2}$ :

$$
K S=I \oplus N_{2}
$$

- After that, $A L$ uses its $N_{2}$ to calculate the following value:

$$
h\left(K \| N_{2}\right)
$$

- Then, $A L$ checks whether $K$ is valid or not using $L$ :

$$
h\left(K \| N_{2}\right) \stackrel{?}{=} L
$$

Step $8: A L \rightarrow P M:\{M, N\}$

- If $K$ is valid, then $A L$ will extract $N_{1}$ from $K$ by using its $N_{2}$ :

$$
N_{1}=K \oplus N_{2}
$$

- Then, $A L$ sores the session key, $K S$, into the parameter $M$ :

$$
M=K S \oplus N_{1}
$$

- $\quad A L$ also computes the parameter $N$

$$
N=h\left(M \| N_{1}\right)
$$

- and send $M, N$ to $P M$

Step 9 : $P M$ gets the session key, $K S$

- $\quad P M$ receives $M, N$ from $A L$
- $\quad P M$ then uses his/her $N_{1}$ to calculate:

$$
h\left(M \| N_{1}\right)
$$

- $\quad P M$ determines whether $M$ is valid or not sent from $A L$ :

$$
h\left(M \| N_{1}\right) \stackrel{?}{=} N
$$

- If $M$ is valid, then $P M$ uses his/her $N_{1}$ to extract the session key, $K S$ from $M$ :

$$
K S=M \oplus N_{1}=h\left(N_{1} \oplus h_{k}(x) \| N_{2}\right)
$$

Hereafter, the session key, $K S=h\left(N_{1} \oplus h_{k}(x) \| N_{2}\right)$ will be used by the mobile user $P M$ and the foreign agent $A L$, to secure their communication.

Table 3. Login and Registration Phase

| PM | AL | AA |
| :---: | :---: | :---: |
| Enters $I D_{P M}, P W_{P M}$ <br> Calculates: $\begin{aligned} & A=h\left(P W_{P M} \\| b\right) \\ & B=h\left(A \\| I D_{P M}\right) \oplus C \end{aligned}$ <br> Checks: $h(B) \stackrel{?}{=} D$ <br> Generates $N_{1}$ <br> Computes: $\begin{aligned} & E=N_{1} \oplus B \\ & F=h(E \\| B) \\ & \quad\{E, F, x\} \end{aligned}$ <br> Step 1 \& 2 | Generates $N_{2}$ <br> Calculates: $\begin{gathered} G=N_{2} \oplus h_{k}\left(I D_{A L} \\| w\right) \\ H=F \oplus h\left(G \\| h_{k}\left(I D_{A L} \\| w\right)\right) \\ \quad\{E, G, H, w, x\} \end{gathered}$ <br> Step 3 | Checks: $\begin{aligned} & h\left(E \\| h\left(I D_{A A} \\| h_{k}(x)\right)\right) \\ & \quad \oplus h\left(G \\| h_{k}\left(I D_{A L} \\| w\right)\right) \stackrel{?}{=} H \end{aligned}$ <br> Calculates: $\begin{aligned} & N_{1}=E \oplus h\left(I D_{A A} \\| h_{k}(x)\right) \\ & N_{2}=G \oplus h_{k}\left(I D_{A L} \\| w\right) \end{aligned}$ Generates session key: |



### 4.3. Update Password Phase

In this phase, mobile user, $P M$ can freely update or change their desired password, hence the authentication scheme is user-friendly. The mobile user inserts their smart card $K P$ into their mobile device. After that, the mobile user enters their old password $P W_{P M}$ as well as their identity $I D_{P M}$. Then, smart card $K P$ determines whether the $P M$ is a valid owner or not. Finally, the old $C$ will be replaced with the new one i.e $C^{\prime}$. The details is explained as follows and depicted in Table 4.
Step 1 : Checks whether $P M$ is the valid owner of $K P$ or not.

- $\quad P M$ enters their old password $P W_{P M}$, and $I D_{P M}$.
- $\quad K P$ calculates $A$ by using $b$ stored inside it:

$$
A=h\left(P W_{P M} \| b\right)
$$

- Then, $K P$ calculates $B$ by using $A$ and $C$ stored inside it:

$$
B=h\left(A \| I D_{P M}\right) \oplus C
$$

- $\quad K P$ determines whether $B$ valid or not using the following equation:

$$
h(B) \stackrel{?}{=} D
$$

- If the equation hold, then $P M$ is the owner of $K P$.

Step 2 : Changing the old password to new password, $P W_{P M}^{\prime}$

- $\quad P M$ can enter the new password, $P W_{P M}^{\prime}$.
- $K P$ calculates:

$$
A^{\prime}=h\left(P W_{P M}^{\prime} \| b\right)
$$

- Then, $K P$ computes the new $C$ and stores it into the parameter $C^{\prime}$ :

$$
C^{\prime}=h\left(A^{\prime} \| I D_{P M}\right) \oplus h\left(A \| I D_{P M}\right) \oplus C
$$

- $\quad K P$ deletes the old $C$ and stores $C^{\prime}$.
- Therefore, the smart card $K P$ now has these parameters stored inside it; $C^{\prime}, D, h(), x,$.

Table 4. Update Password Phase


## 5. Security Analysis

Attack scenarios was employed to demonstrate that the proposed scheme was capable of withstanding possible threats. Assume that Eve, the attacker, can intercept and eavesdrop on the messages transmitted over public communication between the user, the foreign agent, and the home agent. The security assessments are shown in the sections to come.

### 5.1.Smart Card Loss Attack

Assume that Eve stole or found the lost smart card, and she has the ability to extract the secret parameters stored inside the smart card. Notice that the parameters that are stored in the smart card, $K P$, are $C, D, h(), x,$.$b . Recall that the parameters C$ and $D$ are:

$$
\begin{aligned}
& A=h\left(P W_{P M} \| b\right) \\
& B=h\left(I D_{A A} \| h_{k}(x)\right) \\
& C=h\left(A \| I D_{P M}\right) \oplus B \\
& D=h(B)
\end{aligned}
$$

There are three scenarios where Eve can utilize the parameters $C, D, h(), x,$.$b for her benefit:$

1. Use $C, D, h($.$) to bypass step 1$ in the login and authentication phase. In step $1, K P$ needs to verify the smart card owner. Eve can be verified if the equation $h(B)=D$ hold. Thus, Eve must get the parameter $B$. Observe that Eve can extract $B$ from $C$ that is being stored inside $K P$. To decrypt $C$, Eve needs $h\left(A \| I D_{P M}\right)$. However, Eve does not have any information about $I D_{P M}$ and $A$ because only the real owner of the $K P$ knows the valid $I D_{P M}$ and $P W_{P M}$ to compute $A$. Therefore, Eve failed to pass through step 1 in the login and authentication phase. Hence, the login and authentication phase failed to proceed.
2. Assume that Eve uses $h($.$) and b$ to change passwords in the update password phase. In this phase, $K P$ will determine whether the equation $h(B)=D$ satisfied or not before Eve can proceed to change the old password. However, Eve does not have a valid $B$ because she does not have $I D_{P M}$ and $P W_{P M}$. Hence, Eve failed to change the actual user's password.
3. Assume that Eve tries to decrypt $D$ to get $B$. Nevertheless, Eve cannot decrypt $D=h(B)$ because it is hard or almost impossible to decrypt a hash function (the often-used hash function in the real world is SHA-256). Eve may try to find $B^{\prime}$ such that $h\left(B^{\prime}\right)=D$, but she might not be able to find one because a hash function is a collision-free function. Also, if Eve tries to guess $B$ where $B=h\left(I D_{A A} \| h_{k}(x)\right)$ such that $h(B)=D$, she will fail since she does not have the secret key $k$ (only known by $A A$ ).
Therefore, the proposed key agreement scheme can resist a smart card loss case.

### 5.2. Replay Attack

A replay attack occurs when Eve sends back stolen messages to the actual mobile user to get information about the session key. There are two scenarios that allow Eve to steal the transmitted messages between the mobile user, foreign agent, and home agent.

1. Assume that Eve stole $\{E, F, x\}$ in step 2 , login and authentication phase. Eve sends $\{E, F, x\}$ back to the $A A$ to get the session key used by the $P M$ and $A L$. When the $A A$ sends back $\{I, J, K, L\}$ to $A L$, and $A L$ sends back $\{M, N\}$ to Eve, Eve will fail to decrypt $M$ such that $M=K S \oplus N_{1}$ to get the session key $K S$. This is because Eve does not have $N_{1}$. If Eve wants the value of $N_{1}$, then she needs to decrypt $E$ where $E=N_{1} \oplus B$. However, Eve will fail again because she does not have $B$. Thus, Eve cannot generate a session key used by $P M$ and $A L$.
2. Assume that Eve stole $\{E, G, H, w, x\}$ in step 3, login and authentication phase. Then, Eve sends back this message to $A A$. When $A A$ sends back $\{I, J, K, L\}$ to Eve, Eve will fail to decrypt $I$ where $I=K S \oplus N_{2}$ to get the session key $K S$ because Eve does not have $N_{2}$. Moreover, Eve will fail to decrypt $K$ where $K=N_{1} \oplus N_{2}$ to get $N_{1}$ or $N_{2}$ since Eve does not have either one of them.
Therefore, based on the analysis above, the proposed key agreement scheme can resist a replay attack.

### 5.3. Man-in-the-Middle Attack

In a man-in-the-middle attack, Eve acts as a middleman between the mobile user $P M$ and foreign agent $A L$, or between foreign agent $A L$ and home agent $A A$. Eve steals and modifies the message transmitted between the entities. There are two situations where this attack can occur.

1. Assume that Eve acts as a middleman between $P M$ and $A L$, and steals the messages $\{E, F, x\}$ where $E=N_{1} \oplus B, \quad F=h(E \| B)$ in step 2, login and authentication phase. Eve then modifies the message $\left\{E^{\prime}, F^{\prime}, x^{\prime}\right\}$ and forwards it to $A L$. Note that $F^{\prime}$ here not $F^{\prime}=h\left(E^{\prime} \| B\right)$. This is because Eve does not have the valid parameter of $B$ where $B=h\left(I D_{A A} \| h_{k}(x)\right)$ such that Eve can generate $F^{\prime}=h\left(E^{\prime} \| B\right)$. After that, $A L$ sends back the message $\left\{E^{\prime}, G, H^{\prime}, w, x^{\prime}\right\}$ where $G=N_{2} \oplus h_{k}\left(I D_{A L} \| w\right), H^{\prime}=F^{\prime} \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right)$ to $A A$. However, as soon as the $A A$ takes the parameter $E^{\prime}, x^{\prime}, G$ alongside with $h_{k}(),. I D_{A A}$ and $h_{k}\left(I D_{A L} \| w\right)$ that stored in $A A$ then computes $h\left(E^{\prime} \| h\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)\right) \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right), A A$ will get this inequality; $h\left(E^{\prime} \| h\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)\right) \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right) \neq H^{\prime}$. Note that $H^{\prime}$ here is $H^{\prime}=F^{\prime} \oplus h(G \|$ $\left.h_{k}\left(I D_{A L} \| w\right)\right)$ and $F^{\prime}$ not equal to $h\left(E^{\prime} \| h\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)\right.$. This is because Eve does not have the secret key $k$ that can allow her to alter $F^{\prime}$ into $F^{\prime}=h\left(E^{\prime} \| h\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)\right.$. Thus, $A A$ will immediately terminate this session.
2. Assume that Eve acts as a middleman between $A L$ and $A A$ and steals the message $\{E, G, H, w, x\}$ in step 3, login and authentication phase. Eve then modifies $\{E, G, H, w, x\}$ into $\left\{E^{\prime}, G^{\prime}, H^{\prime}, w^{\prime}, x^{\prime}\right\}$ and forwards $\left\{E^{\prime}, G^{\prime}, H^{\prime}, w^{\prime}, x^{\prime}\right\}$ to the $A A$. The $A A$ takes $E^{\prime}, G^{\prime}, w^{\prime}, x^{\prime}$ and computes $h\left(E^{\prime} \|\right.$
$\left.h\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)\right) \oplus h\left(G^{\prime} \| h_{k}\left(I D_{A L} \| w^{\prime}\right)\right)$. However, $A A$ will find that the equation is not equal to $H^{\prime}$ because $H^{\prime}$ does not contain the valid $h_{k}\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)$ and $h_{k}\left(I D_{A L} \| w^{\prime}\right)$. This is because Eve does not have the secret key $k$ to generate the correct $h_{k}\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)$ and $h_{k}\left(I D_{A L} \| w^{\prime}\right)$ which are necessary to modify $E^{\prime}, G^{\prime}$, and $H^{\prime}$. Therefore, $A A$ will immediately terminate this session.

Hence through the analysis above, the key agreement scheme secured against a Man-in-the-middle attack.

### 5.4. Impersonation Attack

There are three scenarios that can occur. Firstly, Eve might impersonate the mobile user $P M$. Secondly, Eve can impersonate the foreign agent $A L$. Thirdly, Eve can impersonate the home agent $A A$. The detail of each situation is as follows:

1. Assume that Eve impersonates the mobile user $P M$. Therefore, Eve needs a valid the $P M$ 's password $P W_{P M}$ and his/her identity $I D_{P M}$. Moreover, Eve needs the $P M$ 's smart card $K P$ to allow her to $\log$ in to $A L$. In addition, the parameters stored inside $K P$ are required to allow Eve to pass through the authentication phase. With these limitations, Eve cannot successfully log in to $A L$ because she does not have the correct $P W_{P M}$ and $I D_{P M}$. Besides that, Eve does not have $K P$. If Eve steals the $P M$ 's smart card $K P$, Eve still not be able to pass through the authentication process because the scheme can resist smart card loss (see section 5.1)
2. Next, assume that Eve impersonates $A L$. However, every $A L$ have its unique $w$. Also, $A A$ computes $h_{k}\left(I D_{A L} \| w\right)$ by using its secrete key $k$ distributes $h_{k}\left(I D_{A L} \| w\right)$ to each $A L$, specifically. This process is assumed to have occurred before the login and authentication phase. Therefore, if Eve wants to impersonate $A L$, Eve will receive $\{E, F, x\}$ from $P M$ in step 2, login and authentication phase. Then, Eve will generate her nonce $N_{2}^{\prime}$ and $w^{\prime}$ to calculate $G^{\prime}=$ $N_{2}{ }^{\prime} \oplus h_{k}\left(I D_{A L} \| w^{\prime}\right)$ and $H^{\prime}=F \oplus h\left(G \| h_{k}\left(I D_{A L} \| w^{\prime}\right)\right)$. However, when $A A$ checks the equation $h\left(E^{\prime} \| h\left(I D_{A A} \| h_{k}\left(x^{\prime}\right)\right)\right) \oplus h\left(G^{\prime} \| h_{k}\left(I D_{A L} \| w^{\prime}\right)\right), A A$ will detect that this equation is not equal to $H^{\prime}$. This is because Eve does not have the secret key $k$ to generate $h_{k}\left(I D_{A L} \| w^{\prime}\right)$.
3. Assume that Eve impersonates $A A$. Eve will receive $\{E, G, H, w, x\}$ from $A L$ in step 3, login and authentication phase. However, Eve is not able to extract $N_{1}$ and $N_{2}$ from the parameter $E=$ $N_{1} \oplus h\left(I D_{P M} \| h_{k}(x)\right)$ and $G=N_{2} \oplus h_{k}\left(I D_{A L} \| w\right)$, respectively. This is because Eve does not have the secrete key $k$ to compute $h\left(I D_{P M} \| h_{k}(x)\right)$ and $h_{k}\left(I D_{A L} \| w\right)$. If Eve wants to send a fake $\left\{I^{\prime}, J^{\prime}, K^{\prime}, L^{\prime}\right\}$ which initially are $I=K S \oplus N_{2}, J=h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right), K=N_{1} \oplus N_{2}$, and $K=N_{1} \oplus N_{2}$ to $A L$, Then the equation $h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right)$ no longer equal to $J$ since $J^{\prime}$ does not contain the valid $h_{k}\left(I D_{A L} \| w\right)$. Thus, $A L$ will immediately terminate this session, and the session key $K S$ cannot be derived from $I^{\prime}$.
Hence, the proposed key agreement scheme is secure against impersonation attacks.

### 5.5.Perfect Forward Secrecy

In the login and authentication phase, the generated session key $K S=h\left(N_{1} \oplus h_{k}(x) \| N_{2}\right)$ is contains with the nonces $N_{1}$ and $N_{2}$. In every new round, $P M$ and $A L$ will always change the nonces $N_{1}$ and $N_{2}$. Therefore, the session key $K S=h\left(N_{1} \oplus h_{k}(x) \| N_{2}\right)$ will also change depending on the new $N_{1}$ and $N_{2}$. Hence, even though Eve successfully obtained the session key $K S=h\left(N_{1} \oplus h_{k}(x) \|\right.$ $N_{2}$ ) in one session, she only can use it in that session. Thus, Eve cannot decrypt the previous messages shared between $P M$ and $A L$. In conclusion, the proposed key agreement scheme can resist various attacks from unauthorized parties.

## 6. Discussions

In this section, the performance and efficiency of the key agreement scheme are analyzed. The scheme was proven to satisfy the important requirements for a secure and efficient key agreement
scheme, namely mutual authentication, user-friendly, anonymity, and low computational cost. The proof for each requirement below is presented below.

### 6.1.Mutual Authentication

In the login and authentication phase, the mobile user $P M$ first sends $\{E, F, x\}$ where $E=$ $N_{1} \oplus B$ and $F=h(E \| B)$ to the foreign agent $A L$ whenever they want to communicate with the home agent $A A$. $A L$ then receives the message $\{E, F, x\}$ from $P M$. After that, $A L$ computes $G=$ $N_{2} \oplus h_{k}\left(I D_{A L} \| w\right)$ and uses $E$ and $F$ to calculate $H=F \oplus h\left(G \| h_{k}\left(I D_{A L} \| w\right)\right)$. Note that the parameter $H$ contains $E, F$, and $G$. Thus, if $A A$ checks the validity of $H, A A$ will also check the validity of $E, F, G$ as well. Hence, $A A$ can check that the $P M$ is a valid user. Furthermore, $A A$ sends $\{I, J, K, L\}$ to $A L$ where $I=K S \oplus N_{2}, J=h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right), K=N_{1} \oplus N_{2}$ and $L=h\left(K \| N_{2}\right)$. Then, $A L$ uses the received $I$ and its $h_{k}\left(I D_{A L} \| w\right)$ to computes $h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right)$ to verify $J$. Therefore, $A L$ is able to make sure that the $A A$ is a valid home agent. This is because if $h\left(I \| h_{k}\left(I D_{A L} \| w\right)\right) \neq J$, then $A A$ is not an authorized home agent because only $A A$ knows $h_{k}\left(I D_{A L} \| w\right)$ to calculate the correct $J$. Apart from that, $A L$ also can verify $L$ by determining whether $h\left(K \| N_{2}\right)=L$ or not. If the equality holds, then $A L$ can proceed to decrypt $K$ by using its $N_{2}$ to obtain $N_{1}$. In this situation, $A L$ sure that $N_{1}$ is valid. Moreover, $A L$ uses the $N_{1}$ to encrypt $K S$ such that $M=K S \oplus N_{1} . A L$ also calculates $N=h\left(M \| N_{1}\right)$ then sends $\{M, N\}$ to $P M . P M$ will use his/her $N_{1}$ and the received $M$ to compute and determine whether $h\left(M \| N_{1}\right)=N$. If it is equal, then $P M$ is sure that $A L$ is a valid foreign agent because only $A L$ who knows the correct $N_{1}$ which is used to generate $N=h\left(M \| N_{1}\right)$. Therefore, $P M$ can authenticate $A A$ because the actual $N_{1}$ received by $A L$ is from $A A$. Hence, through the scenarios above, $P M, A L$, and $A A$ can authenticate each other.

### 6.2. User-Friendly

In this section, the performance and efficiency of the key agreement scheme is analyzed. It is proven that the scheme satisfied the important requirements for a secure and efficient key agreement scheme, namely mutual authentication, user-friendly, anonymity, and low computational cost. The proof for each requirement below is presented below.

### 6.3.Anonymity

The proposed key agreement scheme satisfied the anonymity property. Observe the message sent in step 2, the login and authentication phase. In step 2, the message sent is $\{E, F, x\}$ where $E=$ $N_{1} \oplus B=N_{1} \oplus h\left(I D_{A A} \| h_{k}(x)\right)$ and $F=h(E \| B)=h\left(E \| h\left(I D_{A A} \| h_{k}(x)\right)\right.$. It can be seen that no user's identity is involved in the message. Suppose an unauthorized party somehow obtained the smart card and is able to access all the parameters stored inside it. In that case, he/she cannot extract the user's identity stored in parameter $C$ because he/she does not have the password $P W_{P M}$. In addition, $C$ is encrypted by a secure hash function. Therefore, no user identity can be extracted or exposed to an unauthorized party; hence user anonymity is achieved.

### 6.4. Low Computational Cost

Computational cost is an important aspect in the development of a key agreement scheme. This is because mobile devices such as mobile phones, smart watches, smart cards, Ipad, etc., do not have the capability to handle complex and tedious calculations due to limited computational power. Besides that, a tedious and complex calculation requires a large battery capacity and can exhaust the mobile device's sensors. Therefore, a key agreement scheme based only on low-cost cryptographic primitive, namely XOR operations, keyed one-way hash function, and one-way hash function to reduce the computational tediousness and complexity is proposed. The number of operations involved in the scheme with the scheme proposed by Cheng Guo dan Chin-Yu Sun [16] are compared. The notations involved are listed in Table 5.

Table 5. Notations

| Notations | Descriptions |
| :--- | :--- |
| $H$ | Hash function |
| $X$ | XOR operation |
| $A A$ | Home agent |
| $A L$ | Foreign agent |
| $P M$ | Mobile user |

The comparison of the number of operations involved in the proposed key agreement scheme with the scheme proposed by Cheng Guo dan Chin-Yu Sun is given in Table 6 below.

Table 6. Comparison of the Number of Operations

| Operations | Entities | Our scheme | Cheng Guo \& Chin-Yu Sun's scheme |
| :--- | :---: | :---: | :---: |
| $H$ | $P M$ | 12 | 12 |
|  | $A A$ | 18 | 25 |
|  | $A L$ | 7 | 9 |
| $X$ | $P M$ | 6 | 18 |
|  | $A A$ | 7 | 13 |
|  | $A L$ | 5 | 7 |

Based on Table 6, the mobile user only needed to execute six XOR operations compared to 18 XOR operations in Cheng-Guo and Chin-Yu Sun's scheme. Moreover, the home and foreign agents are only required to perform fewer hash functions and XOR operations than Cheng-Guo and Chin-Yu Sun's scheme. Therefore, the decrement in the number of operations required to be done by each entity will reduce the tediousness and complexity of the calculations involved in the proposed scheme. This will save the mobile device's battery consumption, computational power, and sensor.

## 7. Conclusion

This work presents an improved key agreement scheme from the previous scheme [16] of wireless network authentication. Based on the results in Section 6, the proposed authentication scheme can withstand the most well-known attacks, such as replay attacks, man-in-the-middle attacks, and impersonation attacks, and achieve absolute forward secrecy simultaneously. Moreover, an attacker would still be unable to utilize the parameters stored in the smart card even though they gain access to the smart card because the proposed scheme is an anti-smart card loss attack. Furthermore, the scheme is easy to use, cryptographically secure, and has a minimal computational cost. In addition, neither asymmetric nor symmetric encryption or decryption methods are used. Instead, a low-cost cryptographic primitive is used. Therefore, the authentication scheme is more efficient as well as cryptographically secure.

Based on the results presented in Table 6, Section 6.4 shows that the scheme still requires the mobile user to compute the same number of the hash function as in the Cheng-Guo and Chin-Yu Sun's scheme. Hence, there is still improvement that can be made in the proposed scheme in further study.

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